# Marshall University

# College of Science

# **Mathematics Department**

# MTH 121B: Concepts and Applications with Algebra Review (CT)

#### **Course catalog description**

A quantitative reasoning skills course for non-science majors. Topics include logical thinking, problem solving strategies, beginning statistics and probability, exponential and logarithms modeling, formula use, with basic algebra review.

#### **Credit hours**

4 hours

#### **Prerequisites**

ACT Math 17 or 18, or equivalent Critical thinking (CT) designator

This course carries a CT designator, and students who complete the course receive 3 hours of CT credit towards their general education requirements.

### **List of topics**

- Introduction to quantitative literacy
- Logical thinking
- Fallacies of relevance
- Fallacies of numbers and statistics
- Problem solving through unit analysis
- Problem solving strategies
- Systems of standardized units; rounding numbers
- Scientific notation, order of magnitude
- Scaling factors

- Uncertainty
- Applications in large numbers and unit analysis
- Relations; rates of change
- Linear equations; creating linear models
- Counting techniques
- Probability theory
- Expected valued and the binomial probability formula
- Statistics; graphing statistical data
- Measures of central tendency; normal distribution
- · Sample issues in statistical research
- Exponential growth
- Applications of exponential models
- Using formulas
- Logarithmic scales
- Financial formulas

#### **Learner outcomes**

#### **Introduction-** Students will be able to:

- define quantitative literacy;
- recognize the importance of quantitative literacy in their lives;
- discuss several misconceptions about mathematics.

# **Logical Thinking-** Students will be able to:

- know the difference between a deductive and inductive argument;
- be able to test if a deductive argument is valid or invalid;
- determine if a valid argument is sound or unsound.
- · determine if an inductive argument is weak or strong;
- use truth tables to determine the truth value of a compound proposition;
- use Venn diagrams to determine the validity of a deductive argument.

Fallacies of Relevance - Students should be able to:

 define "fallacy" and recognize many different common fallacies.

#### Fallacies of Number and Statistics- Students should be able to:

- distinguish between necessary and sufficient cause;
- define and use the concepts of absolute and relative change.

#### **Problem Solving through Unit Analysis-** Students should be able to:

- use appropriate units to assist them in problem solving;
- apply Polya's four-step procedure for solving problems.

#### Problem Solving Strategies - Students should be able to:

- Students should recognize that not every problem can be solved using the four-step procedure;
- Students should be able to solve certain problems that they haven't seen before by carefully thinking them through.

# **Systems of Standardized Units; Rounding Numbers-** Students should be able to:

- convert commonly used units from the US Customary System to the Metric System and vice versa;
- round numbers.

#### **Scientific Notation; Order of Magnitude-** Students should be able to:

- change large or small numbers to scientific notation;
- make simple estimates using the four-step procedure for problem solving;
- determine order of magnitude estimates.

# Scaling Factors- Students should be able to:

- measure a distance on a map or model and determine the actual distance or size using the given scale;
- put large numbers in perspective using different techniques.

#### **Uncertainty-** Students should be able to:

- determine uncertainty ranges that derive from measurements and be able to state a level of confidence in the measurement;
- determine the number of significant digits for measurements and exact numbers;
- combine approximate numbers;
- interpret the graphs that are commonly found in weekly news magazines.

#### **Applications in Large Numbers and Unit Analysis-** Students should be able:

 to use the quantitative skills developed earlier to solve problems.

#### **Relations; Rates of Change-** Students should be able to:

- identify the independent and dependent variables in a relation;
- draw the graphs of relations and use relations as models of real world problems;
- determine the slope of a linear relation and be able to graph a linear relation.

# **Linear Equations; Creating Linear Models-** Students should be able to:

- solve linear equations with numbers;
- solve literal linear equations;
- make a linear model from two or more data points.

# **Counting Techniques-** Students should be able to:

- use the Multiplication Principle;
- compute the number of arrangements possible allowing repetition;
- compute simple permutations;
- compute simple combinations;
- know when to apply each idea.

# **Probability Theory**- Students should be able to:

• compute probabilities for independent events, dependent events, mutually exclusive events, non-mutually exclusive events using a priori techniques.

# **Expected Values and Binomial Probability Formula-** Students should be able to:

- compute the expected value;
- compute the probability of success in an experiment.

#### **Statistics; Graphing Statistical Data-** Students should be able to:

- explain the difference between inferential and descriptive statistics;
- interpret data from different types of graphs.

# **Measure of Central Tendency; Normal Distribution-** Students should be able to:

- use the properties of the normal distribution and be able to decide if it is an appropriate model of given data;
- explain how standard deviation and margin of error relate to statistical surveys.

# Sample Issues in Statistical Research- Students should be able to:

• recognize abuses of statistics after studying many examples.

# **Exponential Growth-** Students should be able to:

- explain the difference between exponential growth and linear growth;
- explain why exponential growth cannot continue indefinitely in real world situations;
- solve and interpret doubling time and half-life problems.

#### **Applications of Exponential Models**- Students should be able to:

 use exponential growth and decay models to predict a quantity after any time;

- use exponential growth and decay models to find the time t given the other variables;
- create models of exponential growth or decay from given data points.

#### **Using Formulas-** Students should be able to:

- use given formulas;
- tell if a formula makes sense when described in words or pictures;
- determine the correct units when manipulating a formula.

#### **Logarithmic Scales-** Students should be able to:

- give two examples of natural phenomena whose models are logarithmic;
- solve simple logarithmic equations;
- manipulate common logarithms.

#### Financial Formulas- Students should be able to:

- make a personal budget;
- compute compound interest for the discrete and continuous cases;
- compute the amount in a retirement account;
- compute the monthly car or house payments and understand how accelerating a loan will save on interest.

# Technology

Students must have a calculator that can perform exponentiation (e.g.  $x^y$ ).

# Suggested textbooks

Bennett, *Using and Understanding Mathematics*, 5th edition, ISBN 978-0-321-65279-9

### Last updated

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